Spinodal Superlattices of Topological Insulators

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Supporting Information

ABSTRACT: Spinodal decomposition is proposed for stabilizing self-assembled interfaces between topological insulators (TIs) by combining layers of iso-structural and iso-valent TlBi$_X$ ($X = S$, Se, Te) materials. The composition range for gapless states is addressed concurrently to the study of thermodynamically driven boundaries. By tailoring composition, the TlBiS$_2$−TlBiTe$_2$ system might produce both spinodal superlattices and two-dimensional eutectic microstructures, either concurrently or separately. The dimensions and topological nature of the metallic channels are determined by following the spatial distribution of the charge density and the spin-texture. The results validate the proof of concept for obtaining spontaneously forming two-dimensional TI-conducting channels embedded into three-dimensional insulating environments without any vacuum interfaces. Since spinodal decomposition is a controllable kinetic phenomenon, its leverage could become the long-sought enabler for effective TI technological deployment.

INTRODUCTION

Modern materials technology has been efficiently used to reduce the size and increase the functionality of electronic devices and electrical machinery. Semiconductors find a place in a wide range of applications, such as transistors,¹ detectors,²,³ light emitting diodes,⁴ and lasers,⁵ while powerful permanent magnets are used in renewable power generation and electric motors central to the post-fossil fuel economy.⁶ Many of these technologies require scarce elements to achieve exotic properties, such as the reliance of transparent conductors on indium⁷ or the dependence of permanent magnets on rare earth elements, e.g., dysprosium.⁸,⁹ Similar properties can be replicated by fabrication of heterostructures, where the distinct band structures of the constituent materials facilitates the engineering of electronic properties inside device components. However, this technology relies on artificial growth methods, which increase both the time and the cost of fabrication. Exploring alternative synthesis methods and materials is important for overcoming this challenge.¹⁰

Here, we propose a new approach by combining advanced thermodynamic and electronic structure concepts for novel materials design. The design and manufacture of embedded 2D metallic channels in a 3D insulating matrix will enhance the functionality of scalable circuitry for high-performance electronics. Our approach to obtain these channels exploits easy-to-make self-organizing thermodynamically driven morphologic microstructures. This is an alternative to current efforts, where fabrication of heterostructures has relied mostly

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on artificial growth methods, very likely with thermodynamically unstable or metastable phases.\textsuperscript{11–13} Topological insulators (TIs), which exhibit insulating behavior in bulk and metallic states at their boundaries, are the most promising materials for this purpose.\textsuperscript{14–18} The presence of metallic states relies on the spin–orbit induced band inversion in bulk materials, protected by either time reversal or crystal symmetry.\textsuperscript{17,19} The characteristics of the gaples sb o u n d a r y st a t e s a r el i n e a r dispersion in the bulk band gap, spin texture, robustness against scattering by nonmagnetic impurities, and symmetry protection. Studies have demonstrated that the formation of heterostructures,\textsuperscript{23–26} alloying,\textsuperscript{20,27} and thickness engineering\textsuperscript{28} have advantages for controlling the electronic properties of TIs. In addition, recent studies show that it is possible to observe novel properties in TI superlattices, such as both time reversal and crystal symmetry protected surface states,\textsuperscript{29,30} band structure tuning through a topological phase transition,\textsuperscript{31} topologically nontrivial surface states in a magnetic-TI/TI superlattice,\textsuperscript{3} and the realization of 3D Weyl semimetal phases.\textsuperscript{33} To fully exploit TIs in future devices, a detailed exploration of TI heterostructures/superlattices is needed.

The natural formation of interfaces based on thermodynamic stability is interesting: recent studies have proposed the use of spinodal decomposition to generate materials with ad hoc characteristics which enhance the properties of thermoelectric materials.\textsuperscript{34–37} Spinodal decomposition is a phase separation mechanism, where below the critical temperature $T_c$, the components separate into distinct homogeneous regions with different physical and chemical properties.\textsuperscript{38–40} This allows TI heterostructures consisting of layers of thermodynamically stable phases to be constructed, which is the key to durable and long-lasting applications. Moreover, creating boundaries between chemically distinct but iso-structural phases of some insulating materials has already led to remarkable properties.\textsuperscript{41–46}

The candidate materials, (Tl, Bi)-based ternary chalcogenides, TlBiX$_2$ ($X = S, Se, Te$), are a rare group in which TIs and trivial-insulators share the same crystal structure. TlBiSe$_2$ and TlBiTe$_2$ are 3D TI materials while TlBiS$_2$ is a trivial insulator. These properties allow the investigation of the TI/TI and trivial-insulator/TI boundaries between phases that are both iso-structural (important for forming commensurate interfaces) and iso-valent. Furthermore, TlBiSe$_2$ is a TI similar to Bi$_2$Se$_3$ with the advantage of having an almost perfect Dirac cone at the $\Gamma$-point, which is separated from the bulk states and thus allows for the investigation of the transport properties of the TlBiSe$_2$ boundary states independently of the bulk states.\textsuperscript{44} The topologically trivial system, TlBiS$_2$, has a clear band gap at the surface. Gapless metallic states arise at the onset of the topological phase transition, occurring under strain and/or an external electric field.\textsuperscript{47–49} Another interesting characteristic of this group of materials is the topological phase transition from trivial-insulator to TI resulting from substituting S with Se atoms in TlBi(S$_1-x$Se$_x$)$_2$.\textsuperscript{27} This tunes the lattice constant and spin–orbit coupling (SOC), so that a topological phase transition takes place at the critical point ($x_c \sim 0.48$) and a 3D-Dirac point arises. For $0.6 \leq x \leq 0.9$, gapless surface states appear in the electronic band gap.\textsuperscript{45} In contrast, other independent studies report that the TlBi(S$_1-x$Se$_x$)$_2$ system has gapped surface states for $0.6 \leq x \leq 0.9$,\textsuperscript{50,51} despite being in the topologically nontrivial phase. The physical cause of the opening of the gap is not known, although it is possible that

![Figure 1. Formation enthalpies of the (a) TlBiS$_2$–TlBiSe$_2$, (b) TlBiSe$_2$–TlBiTe$_2$, and (c) TlBiS$_2$–TlBiTe$_2$ structures using DFT calculations (red ●) and cluster expansion technique (green ×) (upper panel). Their respective binodal (orange —) and spinodal curves (brown ---) are illustrated in the lower panels (d–f). The eutectic isotherm, from ref 72 and 73, is illustrated with (green ···).](image-url)
the answer lies in the thermodynamic properties. Additionally, Weyl semimetal phases are predicted for TlBi(Si−Se), and TlBi(Si−Te), alloys at $x = 0.5$ in the case of layer-by-layer growth (Tl−Se(Se+Bi−S) for certain critical values of the $c/a$ ratio. Other interesting phenomena, specifically Rashba spin-splitting and the topological proximity effect, have been observed on the Bi(1 bilayer)/TlBiS$_2$ and Bi(1 bilayer)/TlBiSe$_2$ surfaces, respectively. These interesting properties make this group of materials promising candidates for superlattice studies.

In this work, we combine thermodynamic and electronic structure analysis to define a natural design strategy for TI superlattices that can be an alternative to the very costly and time-consuming experimental artificial growth methods. The current study is built on the following aspects: (i) Identify the miscibility gap of each pair of TlBiX$_2$ ($X = S, Se, Te$) compounds by calculating the thermodynamic phase diagram and predicting the consolute temperature ($T_c$). (ii) Design boundaries between constituent materials to predict appropriate ranges of composition guaranteeing the topologically protected gapless metallic states. (iii) Track the spatial distribution of the charge density of these boundaries to verify the existence of topologically protected 2D metallic channels in the 3D insulating matrix.

## METHODS

### Thermodynamics

The enumeration of configurations, determination of ground state structures, and prediction of energies of more structures through Cluster Expansion are performed within the ATAT framework. The temperature−composition phase boundaries are obtained with Monte Carlo simulations. From this data, using the definition of the Gibbs free energy in ref 10, proper derivatives are calculated to determine the binodal and spinodal loci.

### Bulk

Bulk structures are fully relaxed using the AFLOW high-throughput framework and the DFT Vienna Ab-initio Simulation Package (VASP). Geometry optimizations are performed following the AFLOW standard, using PAW pseudopotentials and the PBE parametrization of the GGA exchange and correlation functional. A high energy-cutoff (40% larger than the maximum cutoff of all pseudopotentials) is used for all calculations. Reciprocal space integration is performed using a mesh of 8000 k-points per reciprocal atom. Structures are fully relaxed (cell volume and ionic positions) until the energy difference between two consecutive ionic steps is smaller than 10$^{-7}$ eV. Electronic structure calculations for TlBiS$_2$, TlBiSe$_2$, and TlBiTe$_2$ are performed with SOC.

### Interfaces

The lattice parameters (stress) and ionic positions (forces) are optimized until all force components on each ion are less than 0.001 eV/Å. The outer s and p electrons are treated as valence electrons with the rest included in the core. A kinetic energy cutoff of 392 eV and a Γ-centered 9 × 9 × 1 k-point mesh is used. Electronic structure calculations are performed with SOC.

## RESULTS AND DISCUSSION

### Thermodynamic Properties

Figure 1a−c illustrates the calculated and predicted formation enthalpies ($\Delta H_f$) from DFT and cluster expansion, respectively. All three systems have positive $\Delta H_f$ for the entire range of compositions (0 < $x$ < 1): these systems are immiscible at 0 K. Cluster expansion predictions well agree with DFT calculated energies with small cross validation scores which are tabulated in Table 1. The miscibility of two isomorphous systems can be addressed using the classic Hume−Rothery rules based on four properties: atomic radius, crystal lattice, valence, and electronegativity. These three systems have the same crystal structure; S, Se, and Te atoms are from the same group in the periodic table and have similar electronegativities, while the atomic radii range from 1.04 Å for S to 1.17 Å for Se and 1.37 Å for Te. This difference creates a mismatch between the constituent lattices, reducing interface coherence, eventually leading to phase decomposition.

Combining the output of the Monte Carlo simulations with a previously developed model enables the inexpensive and efficient prediction of the spinodal curve, a quantity which is not usually calculated. The calculated phase diagrams in Figure 1d−f show that TlBiS$_2$−TlBiSe$_2$, TlBiSe$_2$−TlBiTe$_2$, and TlBiSe$_2$−TlBiTe$_2$ systems have an asymmetric miscibility gap. The asymmetric behavior of the miscibility gap is typical when the substitution atoms of the two end members have very different atomic radii.

The calculations indicate that TlBiS$_2$ and TlBiSe$_2$ are miscible above 162 K (Figure 1d). To the best of our knowledge, for the TlBiS$_2$−TlBiSe$_2$ system, there are no experimentally obtained phase diagrams data available below 930 K, at which temperature both compounds are still completely miscible. Successful high temperature synthesis followed by cooling to room temperature has been reported for several compositions. For these experiments, homogeneity for $x = 0.8$ is indicated at the 8 μm scale by electron probe microanalysis, although it is unclear at which temperature the analysis was performed. Angle-resolved photoemission spectroscopy (ARPES) measurements to investigate the novel electronic properties are performed at very low temperatures, where no thermodynamic data is available. The calculated phase diagram (Figure 1d) indicates that TlBiS$_2$ and TlBiSe$_2$ should start to spinodally decompose when the system is cooled down for ARPES measurements. However, due to slow kinetics at low temperatures, the sample may not have sufficient time to complete the decomposition process prior to the electronic structure measurements. Without reaching equilibrium, different time−temperature profiles will lead to different experimental results. Therefore, depending on the details of the experimental procedure, the samples that the ARPES measurements are performed on could be at different stages of phase separation, which would explain the different results obtained in the two independent electronic structure studies.

For TlBiSe$_2$−TlBiTe$_2$, there are no experimental data available below 760 K. The Monte Carlo simulations show that TlBiSe$_2$ and TlBiTe$_2$ become immiscible below 400 K (Figure 1e). This system is suitable for the practical realization of self-organized heterostructures: It is possible to obtain a homogeneous stable phase around 500 K (well below the melting point of the materials); and to obtain self-organized heterostructures between chemically distinct but iso-structural phases at room temperature. The predicted results show that the TlBiS$_2$−TlBiTe$_2$ system is immiscible below 1040 K. Reported experimental results indicate a eutectic isotherm at $T_c \approx 810$ K. Its range of compositions is depicted in Figure 1 as a horizontal line. There are two scenarios. (i) Any mixture starting outside the eutectic

<table>
<thead>
<tr>
<th>TlBiS$_2$−TlBiSe$_2$</th>
<th>TlBiSe$_2$−TlBiTe$_2$</th>
<th>TlBiS$_2$−TlBiTe$_2$</th>
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<tbody>
<tr>
<td>CV score</td>
<td>$0.63$</td>
<td>$1.15$</td>
</tr>
<tr>
<td>$T_c$</td>
<td>$162.00$</td>
<td>$400.00$</td>
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<td>$x_c$</td>
<td>$0.40$</td>
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solv[\text{TlBi(S$_2$-rich,Te$_2$-poor) or TlBi(S$_2$-poor,Te$_2$-rich)]}
and solidifying through the miscibility gap will not undergo eutectic transformation and eventually will find the spinodal line at lower temperature. (ii) Any composition within the eutectic range will allow a fraction of the liquid to reach $x \sim 64\%$ causing a eutectic transformation. This is an interesting regime: the potentially sudden atomic reorganization, the release of latent heat, and the concomitant entrance in the spinodal region will promote the formation of interesting phase-separating 2D microstructures which can be further tailored through heat treatment (eutectic superlattices). Such organizations could have surprising electronic properties. Experiments at and around the eutectic composition with different time−temperature profiles are highly suggested.

Compositions slightly above the minimum and slightly below the maximum eutectic range could also lead to interesting properties.

Since excess vibrational free energy is neglected in our calculations, lower $T_c$ values can be expected in experiment, and similar behavior is reported for other systems.$^{5,76}$ Also, as a result of the slow kinetics at low temperatures, experimental proof of the miscibility gap has not been reported yet for these systems.

The calculations show that larger mismatches between the size of the interchangeable atoms corresponds to higher $T_c$ values for these three systems. Similar behavior has been observed for various systems, such as refractory carbide solid solutions,$^7$ lead chalcogenides,$^10$ and some carbonate quasibinary systems.$^{77}$

**Boundaries of Immiscible Systems.** Boundaries of immiscible systems are modeled by keeping the phase boundary wavelength, $\lambda_{\text{max}}$, constant. Generally, $\lambda_{\text{max}}$ ranges from 10 to 100 nm for various systems.$^{36,78,79}$ For these calculations, $\lambda_{\text{max}}$ is set to 13–14 nm for computational feasibility. This value also provides sufficient thickness for investigating gapless metallic states.$^{52,80}$

In the crystalline solution, finite thickness regions form and interfaces emerge in between them. Biaxial strain of opposite sign is imposed on both sides of the interface until they reach the mutual lattice parameter. Therefore, the strain is shared between each side of the interface (one compressive and the other tensile) so that the misfit between the lattices is reduced. For small strains, the system remains coherent. However, in the case of large strain, the system interfaces can become semicoherent with periodically repeating misfit dislocations.

In epitaxially grown semiconductor heterostructures, the misfit can be accommodated by uniform elastic strain for films below a critical thickness.$^{81,82}$ Analogously, we propose that coherent interfaces can be obtained in the spinodally decomposed systems, even for big lattice misfits, by keeping one region

![Figure 2](image-url). (a) Schematic representation of considered compositions and (b) band alignment for (TlBiS$_2$)$_{1-x}$(TlBiSe$_2$)$_x$. (c) Spatial distribution of the charge density of states $B_1$ and $B_2$ at $\Gamma$ for $x = 11/18$. The summed charge density of both states is also shown and exhibits a symmetric shape over the whole system. Electronic band structure of (TlBiS$_2$)$_{1-x}$(TlBiSe$_2$)$_x$ boundaries with projection of four atomic layers from each side of the boundaries for compositions (d) $x = 8/18$, (e) $x = 9/18$, (f) $x = 10/18$, (g) $x = 11/18$, (h) $x = 12/18$, and (i) $x = 13/18$. The insets show the band structure with in-plane spin contributions. The sizes of the symbols are proportional to the degree of in-plane spin polarization in the five atomic layers nearest the interface, and the red and blue colors correspond to the in-plane spin-up and spin-down directions, respectively. $\Gamma - \Gamma - M$ represents the path in the two-dimensional Brillouin zone of the rhombohedral lattice.
thinner than the critical thickness. Therefore, the investigation of the large lattice mismatch systems TlBiSe₂/TlBiTe₂ and TlBiS₂/TlBiTe₂ is performed by focusing around the end compositions where one region is very thin. For the moderate lattice mismatch system TlBiS₂/TlBiSe₂, the whole compositional range is investigated.

If the band inversion takes place at \( \Gamma \) in 3D, then the Dirac points will always appear at \( \Gamma \) in 2D, independent of the lattice direction. The superlattices are modeled along the (111) direction of the rhombohedral cell for computational feasibility, while still capturing the relevant physics. Creating boundaries between iso-structural and iso-valent phases eliminates the effect of dangling bonds on the electronic structure due to the continuous nature of the system. For these calculations, the boundaries are placed between the weakly bonded interfacial \( X \)–Tl layers, although these layers are still considered as strongly interacting due to their ionic/covalent bonding. This is in contrast to Bi₃Se₃ and Bi₃Te₃, which have weak van der Waals bonds between quintuple layers.

The superlattices are modeled by considering the 0 K configurations, since the sample cleaving and the ARPES measurements are mostly carried out at low temperatures (~15–30 K). At 0 K, only two separate phases can exist; an interface forms between TlBiS₂ and TlBiSe₂, TlBiSe₂ and TlBiTe₂, or TlBiS₂ and TlBiTe₂.

The band alignment needs to be investigated to define the position of the gapless metallic states and to understand the interaction between the constituent materials bands. First, the average electrostatic potential difference between the two constituent materials is obtained. Next, the difference between the valence band edge and the average electrostatic potential of each constituent material (which is under the same biaxial strain as in the superlattice) is calculated. For each system, the band alignment is investigated for two compositions. The results show that although the band offset magnitude changes, the band alignment character of the system is preserved. This demonstrates the feasibility of engineering the bands of spinodally decomposed materials through compositional tuning.

**Figure 3.** Electronic band structure of \((\text{TlBiSe}_2)_{1-x}(\text{TlBiTe}_2)_x\) boundaries for compositions (a) \( x = 2/18 \), (b) \( x = 3/18 \), (c) \( x = 14/18 \), (d) \( x = 15/18 \), and (e) \( x = 16/18 \). The contributions of four atomic layers from each side of the region or the contribution of the entire thin region (in the case of very thin regions) are projected onto the electronic band structures. (f and h) Projected and isosurface representation of summed charge density for \( x = 2/18 \), 3/18, and 14/18. (g) Schematic representation of band alignment of \((\text{TlBiSe}_2)_{1-x}(\text{TlBiTe}_2)_x\) boundaries for TlBiSe₂-rich and TlBiTe₂-rich compositions. The insets show the band structure with in-plane spin contributions. The sizes of the symbols are proportional to the degree of in-plane spin polarization in the five atomic layers nearest the interface, and the red and blue colors correspond to the in-plane spin-up and spin-down directions, respectively (color code: Bi (red ●); Tl (brown ●); Se (green ●); Te (blue ●)).

\((\text{TlBiSe}_2)_{1-x}(\text{TlBiTe}_2)_x\) **Boundaries.** These boundaries represent a possible trivial-insulator/TI system. In order to find the composition(s) where 2D-gapless metallic states arise, a wide range of composition space is scanned (Figure 2a) while adhering to a constant value of \( \lambda_{\text{max}} \).
The positions of the interface states are illustrated by projecting the contribution of four atomic layers from each side of the boundary. As can be seen in Figure 2, metallic states emerge for the 8/18 ≤ x ≤ 13/18 compositional range, and the system has a tiny band gap (Figure 2d–i), which is smaller than the room temperature thermal energy (0.025 eV) and is within the DFT error range. The atom resolved band structures indicate that the lower branch of the metallic state originates from TlBiSe2 and the upper branch is from TlBiS2. The system has staggered (type-II) band alignment (Figure 2b), where the TlBiS2 conduction band and the upper branch of the TlBiSe2 Dirac cone fall in the same energy range. In fact, the upper branch of the Dirac cone is embedded in the TlBiS2 conduction bands, and the biggest contribution comes from TlBiSe2 at Γ.

Analyzing the projected charge density of the metallic states can provide a better spatial understanding of the electronic structure of the system. This projection is presented in Figure 2c for composition x = 11/18 at Γ, B1, and B2 represent the highest and lowest points of the bands at Γ. For B1, the charge density accumulates around the interfaces with some penetration through the interior layers. This agrees well with the reported studies which indicate that the charge density of the surface states decays much slower for TlBiS2 specifically for TlBiSe2 than for Bi2Se3 and Bi2Te3.85,86,87 For the B2 state, the charge density shifts away from the interface as a result of the interaction between the TlBiSe2 Dirac cone and the TlBiS2 conduction band minimum. This is consistent with previous studies of TI heterostructures, which show that depending on the interaction strength at the interface, the spatial position of the Dirac states can shift away from the interface.85,86,87 The orbital character of the B1 and B2 bands at Γ are mainly p_x, consistent with surface states of TlBiSe2, and different from the p_y orbital character of the valence band maximum and conduction band minimum of the bulk (see Supporting Information). Due to the spatial shift of the B2 state, the total charge density at the Dirac-like point is distributed all over the material instead of accumulating at the interfaces (Figure 2c). It can, however, be expected that for larger superlattices with thicker TlBiS2 regions (larger λ_max), the states will be localized close to the interface. The spin polarized band structure (Figure 2d–i, insets) illustrates that spin degeneracy is lifted for the upper branch of the gapless metallic states, which is from the trivial insulator (TlBiS2), specifically for x = 10/18 and 11/18. This behavior is similar to the recent studies which report that, in semiconductor/TI heterostructures, semiconductor states can acquire a nontrivial spin texture as a result of their interaction with the TI interface states.85,86

(TlBiSe2)_{1−x}(TlBiTe2)_x Boundaries. This system contains two 3D TI materials. The presence of gapless topological interface states at the junction of two TIs depends on the helicity and magnitude of the Fermi velocity of the TI surface states and on the mirror symmetry of the system.85,90 Due to the focus around the end compositions at the TlBiSe2(TlBiTe2)-rich part, the TlBiTe2(TlBiSe2) region becomes quite thin, behaving like an ultrathin film. In addition, the systems have broken band alignment, where the fundamental band gaps of the two constituent materials do not overlap. No interaction is expected between any present TlBiSe2 and TlBiTe2 metallic interface states. However, due to the narrow band gap of the systems, the overlap between the electron and hole states of TlBiSe2 and TlBiTe2 is large. The contribution of four atomic layers from each side of the region or the contribution of the entire thin region (in the case of very thin regions) is projected onto the electronic band structures. This illustrates how changing the composition affects the interface states.

The TlBiX3 systems have ionic/covalent bonding rather than van der Waals bonding between the layers. Interlayer separation changes with respect to bulk at the interface between TlBiSe2 and TlBiTe2, are less than 0.2 Å, indicating that the interaction at the interface remains strong. As a result of this strong interaction, reshaping of the bands is expected. This is different than the simple superposition of bands where interfacial coupling is weak. The band structures for various compositions are presented in Figure 3. It can be clearly seen that, around the two end compositions, one region is thick enough to reproduce the bulk band features. Since the system is periodically repeating and the vacuum interface is neglected, the Dirac cone from the surface states does not show up in the electronic band structure. Therefore, in contrast to the TI heterostructures where vacuum interfaces are considered, multiple Dirac cones are not expected here.85,87

For TlBiSe2-rich compositions (x = 2/18 and 3/18), the TlBiSe2 region is much wider than TlBiTe2 and wider than the theoretically defined critical thickness for the emergence of the Dirac cone. For these compositions the upper branch of the Dirac cone is present near the Fermi level. The lower branch is suppressed by TlBiTe2 bulk states, and no gapless states are present. At x = 2/18, X-shaped gapless metallic states emerge around ~0.85 eV, and these states are mainly from the TlBiTe2 region and mostly localized at the interface (Figure 3f). However, they are topologically trivial states since they have spin degeneracy. A similar X-shaped band is reported for one bilayer Bi on the TlBiSe2 surface.91 At x = 3/18 (Figure 3b), gapless interface states arise around ~0.7 eV at Γ (black ellipse). The isosurface charge density indicates that these states are TlBiSe2 interface states and have p_z character. Also, the spin resolved band structure shows that these bands are spin polarized (Figure 3b, inset). A similar state is reported for other TI superlattices.92,93

At the TlBiTe2-rich compositions, the thickness and relative strains on the regions change. This does not alter the band alignment character and only tunes the band offset. For these compositions, the TlBiTe2 region is thick enough to obtain a Dirac cone from interface states, but the interface states are gapped near the Fermi level, as indicated by the red arrow (Figure 3d). However, Dirac-like gapless states emerge between the TlBiSe2 and the TlBiTe2 states around ~0.5 eV. In order to understand the nature of these states, the projected charge density as well as the isosurface charge density at Γ is presented in Figure 3b for x = 14/18. The plots indicate that these Dirac-like points are spread across the TlBiTe2 interface state and the TlBiSe2 bulk state. These types of bands are reported for TI heterostructures and are described as mixed-character bands.85,87,89 Thusly, instead of two metallic channels, only one metallic channel arises, which includes the entire TlBiSe2 region. The upper and lower branches of the Dirac-like points have opposite spin polarization (Figure 3c–e, insets), indicating that they are topologically protected.

(TlBiS2)_{1−x}(TlBiTe2)_x Boundaries. This system is another example of a possible trivial-insulator/TI system with a large lattice misfit.

In the TlBiS2-rich compositions, the TlBiTe2 region is very thin, so the system is a superlattice of a trivial insulator and an ultrathin film of 3D TI with broken band alignment. The band structures in Figure 4a–c demonstrates that at compositions x...
In this work, the electronic properties of thermodynamically formed topological insulator superlattices have been investigated. Our results demonstrate that it is possible to obtain...
self-assembled interfaces between iso-structural and iso-valent materials with interesting electronic properties. Compositional tuning induces various phenomena, such as topological interface states, spin texture gain by nontopological states, band inversion, band crossing between the TRIM points, and Rashba-like states. The emergence of these phenomena is related to the band alignment and composition of the systems. With this method, we demonstrate that obtaining 2D metallic channels in a 3D insulating matrix is possible for TI superlattices without vacuum interfaces. Since these states are protected from the environment, they can be useful for device applications. These findings suggest that the combination of thermodynamic and electronic properties can create a pathway for investigating thermodynamically driven interfaces to obtain possible novel phenomena, which may help to explore more materials for spintronic devices and further applications.

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