

STEFANO CURTARO 60

- MULTIATOMS
- LCAO
- 2 ATOMS
- 4 ATOMS
- DEBYE - HUCKEL

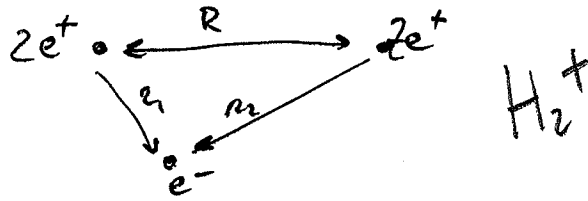
M1 - M16

H1 - H2

MULTIATOMS (MOLECULES)

1e \Rightarrow 2 nuclei

LCAO



$$V(r_1, r_2, R) = e^2 \left[-\frac{1}{r_1} - \frac{1}{r_2} + \frac{1}{R} \right] \Rightarrow$$

FROZEN IONS
BOHR-OPPENHEIMER
R constant \Rightarrow with C.M.
electrons follow \Rightarrow

$$V(r_1, r_2) = e^2 \left[-\frac{1}{r_1} - \frac{1}{r_2} \right] \Rightarrow$$

$$\rightarrow E_{mol} = E_{el}(R) + \frac{e^2}{R}$$

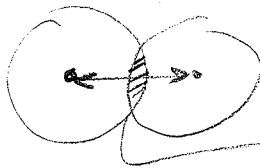
nuclei

function of R because $r_2 = r(r_1, R)$

LCAO : Linear Combination Atomc Orbitals.

$$a_0 \rightarrow \frac{a_0}{Z}$$

$\phi_1 =$ wavefunction of atom 1 $\Rightarrow GS = \frac{1}{\sqrt{\pi a_0^3}} e^{-r_1/a_0} \quad 1s_1$
 $\phi_2 =$ wavefunction of atom 2 $\Rightarrow GS = \rightarrow$



Superposition (R)

$R \downarrow$, super \uparrow , $R \uparrow$, superpas \downarrow
 exponentially

take real for simplicity

$$\psi = c_1 \phi_1 + c_2 \phi_2 \Rightarrow \text{to normalize}$$

$$\hat{H}\psi = E\psi \quad H|\psi\rangle = E|\psi\rangle$$

$$E = \frac{\int \psi^* \hat{H} \psi dV}{\int \psi^* \psi dV} = \frac{\langle \psi | H | \psi \rangle}{\langle \psi | \psi \rangle}$$

$$= \frac{\int (c_1 \phi_1^* + c_2 \phi_2^*) \hat{H} (c_1 \phi_1 + c_2 \phi_2) dV}{\int (c_1 \phi_1^* + c_2 \phi_2^*) (c_1 \phi_1 + c_2 \phi_2) dV} \Rightarrow$$

COULOMB INTEGRALS $H_{ii} \equiv \int \phi_i^* \hat{H} \phi_i dV$
 BOND INTEGRAL $H_{ij} \equiv \int \phi_i^* \hat{H} \phi_j dV$ } for numerators

(SUPERPOSITION) OVERLAP INTEGRAL $S_{ij} = \int \phi_i^* \phi_j dV$ } for DEN
 $S_{ii} = 1$ (no normalization)

same for symmetry

$$\Rightarrow E = \frac{c_1^2 H_{11} + c_2^2 H_{22} + c_1 c_2 (H_{12} + H_{21})}{c_1^2 + c_2^2 + c_1 c_2 (S_{12} + S_{21})}$$

$$H_{12}(R \rightarrow \infty) \rightarrow 0$$

$$S_{12}(R \rightarrow \infty) \rightarrow 0$$

$$E_{LCAO} = \frac{c_1^2 H_{11} + c_2^2 H_{22} + 2c_1 c_2 H_{12}}{c_1^2 + c_2^2 + 2c_1 c_2 S_{12}}$$

Variational principle
solution of the
problem

$$\left(\frac{\delta E}{\delta \psi} = 0 \right) \Rightarrow$$

minimize E
over all possible
choices of ψ
(guesses)

$$\Rightarrow \frac{\partial E}{\partial c_1} = \frac{\partial E}{\partial c_2} = 0 \quad , \text{ minimize}$$

$$\frac{\partial E}{\partial c_1} = 0 \Rightarrow \frac{1}{D} \frac{\partial N}{\partial c_1} - \frac{N}{D^2} \frac{\partial D}{\partial c_1} = 0 \quad * D \neq 0 \Rightarrow \frac{\partial N}{\partial c_1} - E \frac{\partial D}{\partial c_1} = 0$$

$$\Rightarrow 2c_1 H_{11} + 2c_2 H_{12} - E(2c_1 + 2c_2 S_{12}) = 0$$

$$\left\{ \begin{array}{l} c_1 (H_{11} - E) + c_2 (H_{12} - E S_{12}) = 0 \\ c_1 (H_{12} - E S_{12}) + c_2 (H_{22} - E) = 0 \end{array} \right. \quad \text{and } \frac{\partial E}{\partial c_2} = 0 \quad \text{is?}$$

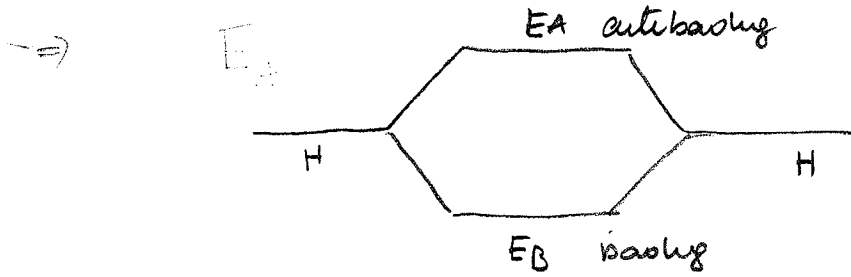
$H = H_{11} + H_{22}$ COULOMB
is identical
for H_2^+

$$\Rightarrow \begin{bmatrix} (H_{11} - E) & (H_{12} - E S_{12}) \\ (H_{12} - E S_{12}) & (H_{22} - E) \end{bmatrix} \begin{pmatrix} c_1 \\ c_2 \end{pmatrix} = 0$$

det() = 0
second order
equation
2 solutions

$$E_A = H + \frac{(H_{12} - H S_{12})}{1 + S_{12}} \quad \uparrow c_1 = -c_2$$

$$E_B = H - \frac{(H_{12} - H S_{12})}{1 - S_{12}} \quad \downarrow c_1 = c_2$$

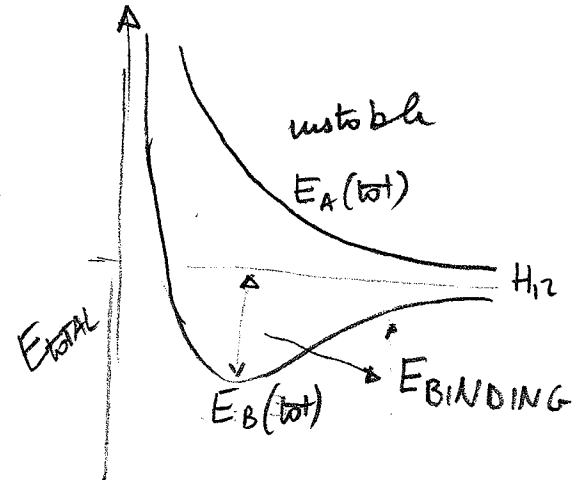
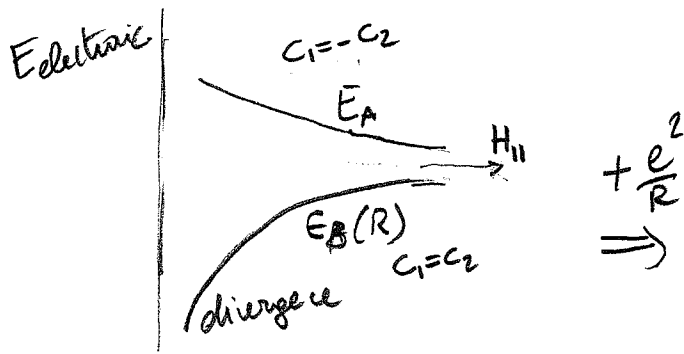


$$H_{12}(R \rightarrow \infty) \rightarrow 0$$

$$S_{12}(R \rightarrow \infty) \rightarrow 0$$

$$S_{12}(R \rightarrow 0) \rightarrow 1$$

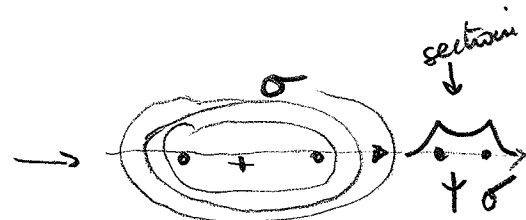
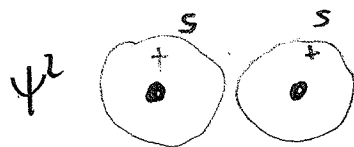
$$S(R \rightarrow 0) \rightarrow 1 \Rightarrow$$



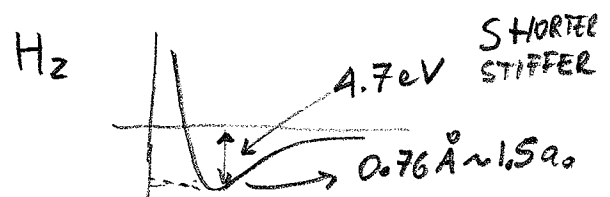
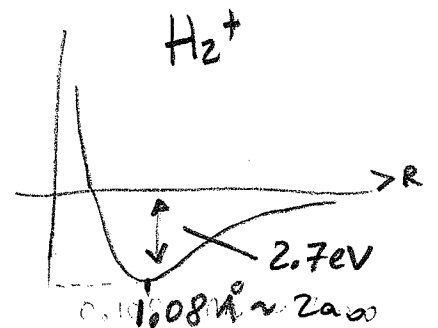
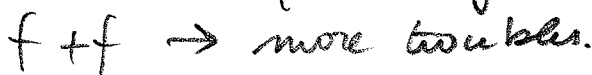
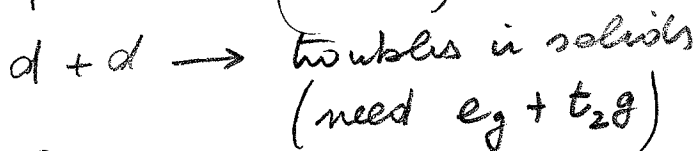
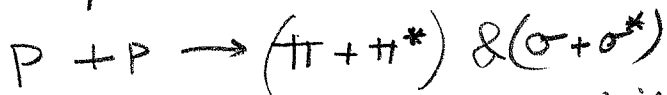
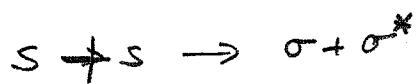
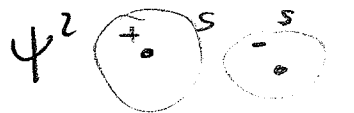
$$\text{total } E = E_{\text{electronic}} + E_{\text{coulomb}}(R)$$

$$= \frac{e^2}{R^*}$$

$$\Psi_B = c_1(\phi_1 + \phi_2)$$

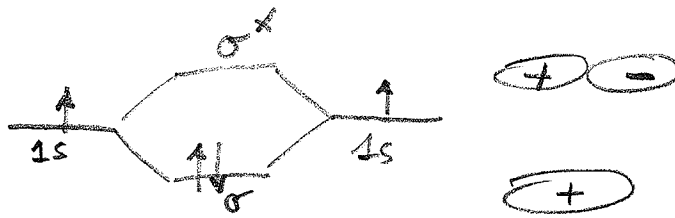


$$\Psi_A = c_1(\phi_1 - \phi_2)$$



LITHIUM

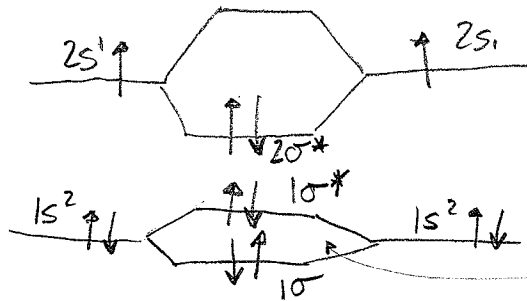
H₂



$$E_A = H. + \frac{(H_{12} - HS_{12})}{1 + S_{12}}$$

$$E_B = H. - \frac{(H_{12} - HS_{12})}{1 - S_{12}}$$

Li₂ 1s² 2s¹



deeper electrons \Rightarrow
 $S(1s) < S(2s) \Rightarrow$
 opening is smaller

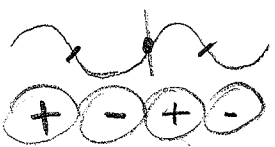
Li₄

max there are 4 atoms

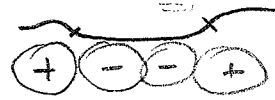


\Rightarrow solution $\Psi = \sum c_i \phi_i$

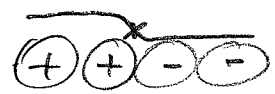
all $c_i > 0$ for
 convention



$$\Psi_4 = c_{41} \phi_1 - c_{42} \phi_2 + c_{43} \phi_3 - c_{44} \phi_4 \quad 3 \text{ nodes } A$$



$$\Psi_3 = c_{31} \phi_1 - c_{32} \phi_2 - c_{33} \phi_3 + c_{34} \phi_4 \quad 2 \text{ nodes } S$$

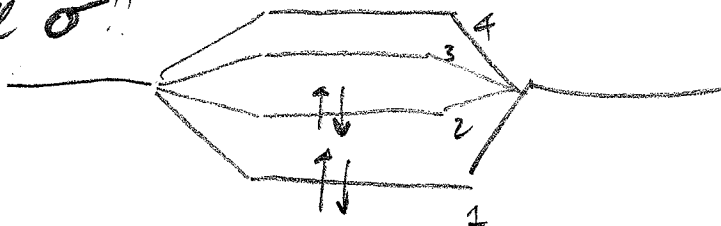


$$\Psi_2 = c_{21} \phi_1 + c_{22} \phi_2 - c_{23} \phi_3 - c_{24} \phi_4 \quad 1 \text{ node } A$$



$$\Psi_1 = c_{11} \phi_1 + c_{12} \phi_2 + c_{13} \phi_3 + c_{14} \phi_4 \quad 0 \text{ nodes } S$$

spherical, all σ !!



N

MORE COMPLICATED STRUCTURES!

LCAO (H_{ii}, H_{ij}, S_{ij}) \implies DEBYE HUCKEL MODEL
(z, β)

$$H_{ii} = \int \phi_i \hat{H} \phi_i dV \xLeftrightarrow{\text{COWMBS}} z \quad \text{all identical atoms}$$

$$H_{ij} = \int \phi_i \hat{H} \phi_j dV \xRightarrow{\text{BOND}} = \begin{cases} z & |i-j|=0 \text{ same} \\ \beta & |i-j|=1 \text{ first neighbours} \\ 0 & \text{elsewhere} \end{cases}$$

$$S_{ij} = \int \phi_i \phi_j dV \xRightarrow{\text{OVERLAP}} = \begin{cases} 1 & |i-j|=0 \text{ normalization} \\ 0 & \text{elsewhere} \end{cases}$$

NO OVERLAP drastic? yes but works

for $H_2 \implies \begin{vmatrix} H_{11} - E & H_{12} - ES_{12} \\ H_{12} - ES_{12} & H_{22} - E \end{vmatrix} \begin{pmatrix} C_1 \\ C_2 \end{pmatrix} = 0 \implies \begin{vmatrix} z - E & \beta \\ \beta & z - E \end{vmatrix} = 0$

$$(z-E)^2 - \beta^2 = 0 \implies E = \frac{z-\beta}{z+\beta}$$

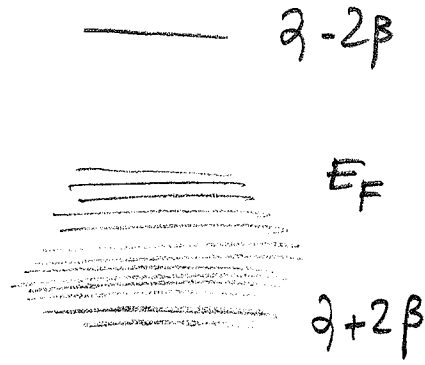
for $L14 \implies \begin{vmatrix} z-E & \beta & 0 & 0 \\ \beta & z-E & \beta & 0 \\ 0 & \beta & z-E & \beta \\ 0 & 0 & \beta & z-E \end{vmatrix} \implies \det = 0$

β is negative

$$E = \begin{matrix} \text{---} & z - 1.6\beta \\ \text{---} & z - 0.6\beta \\ \text{---} & z + 0.6\beta \\ \text{---} & z + 1.6\beta \end{matrix}$$

$N \rightarrow \infty$

$E =$
continuous



Solution

$$\Psi_i = \sum_j c_{ij} \phi_j$$

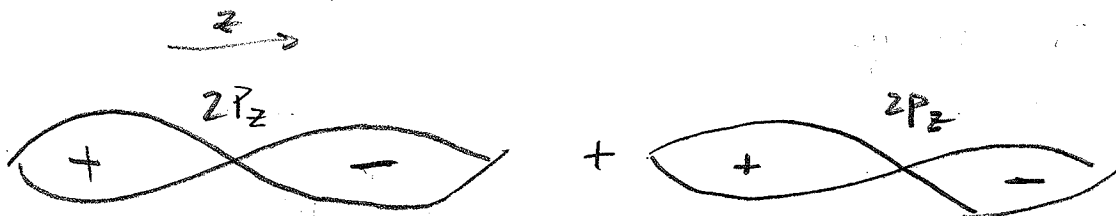
$$c_{ij} = \sqrt{\frac{2}{N+1}} \sin\left(\frac{\pi i j}{N+1}\right)$$

$$E_i = \alpha + 2\beta \cos\left(\frac{\pi i}{N+1}\right)$$

DEBYE
HUCKEL
MODEL.

→ MORE NODES, WIGGLES
⇒ higher energy.

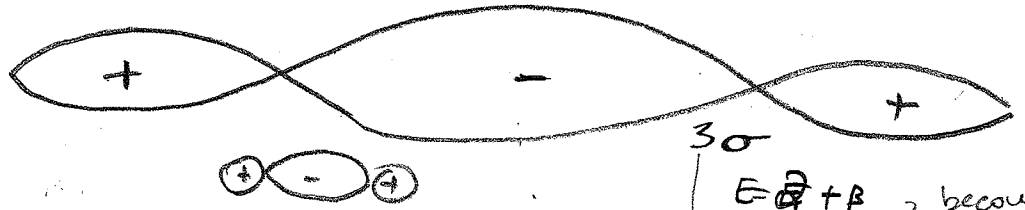
what about if I mix P orbitals?



SYMMETRIC PROBLEM

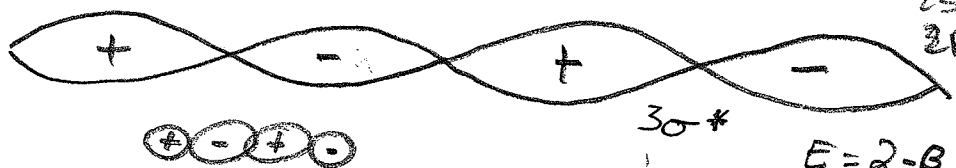
⇒ 2 SOLUTION SYMM & ANTI

SYMM E_σ
lower energy

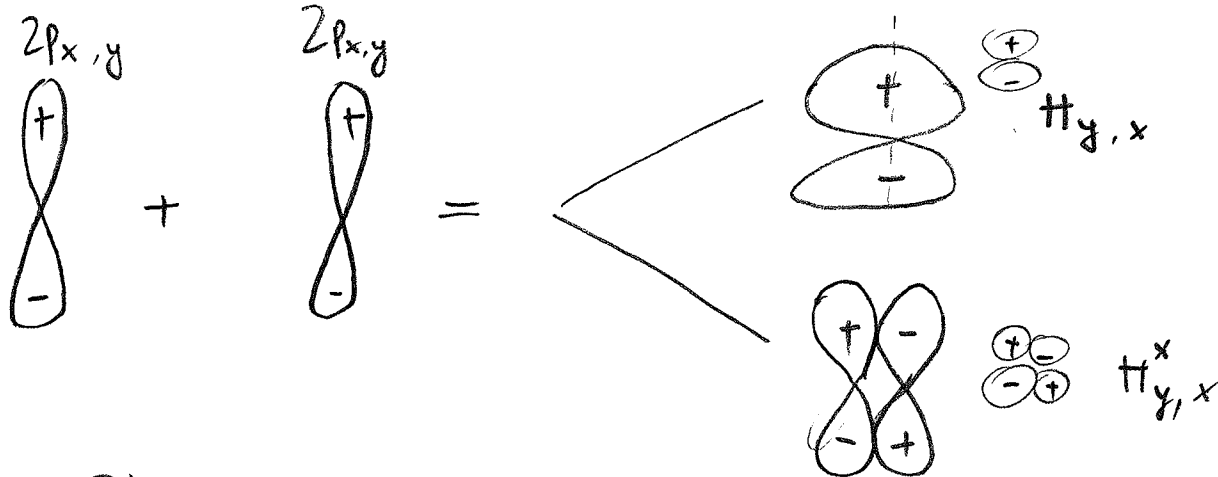


$E = \alpha + \beta$ because
 $1s \rightarrow 1\sigma$
 $2s \rightarrow 2\sigma$
 $2p \rightarrow 3\sigma, 4$

ANTI E_σ
Higher energy

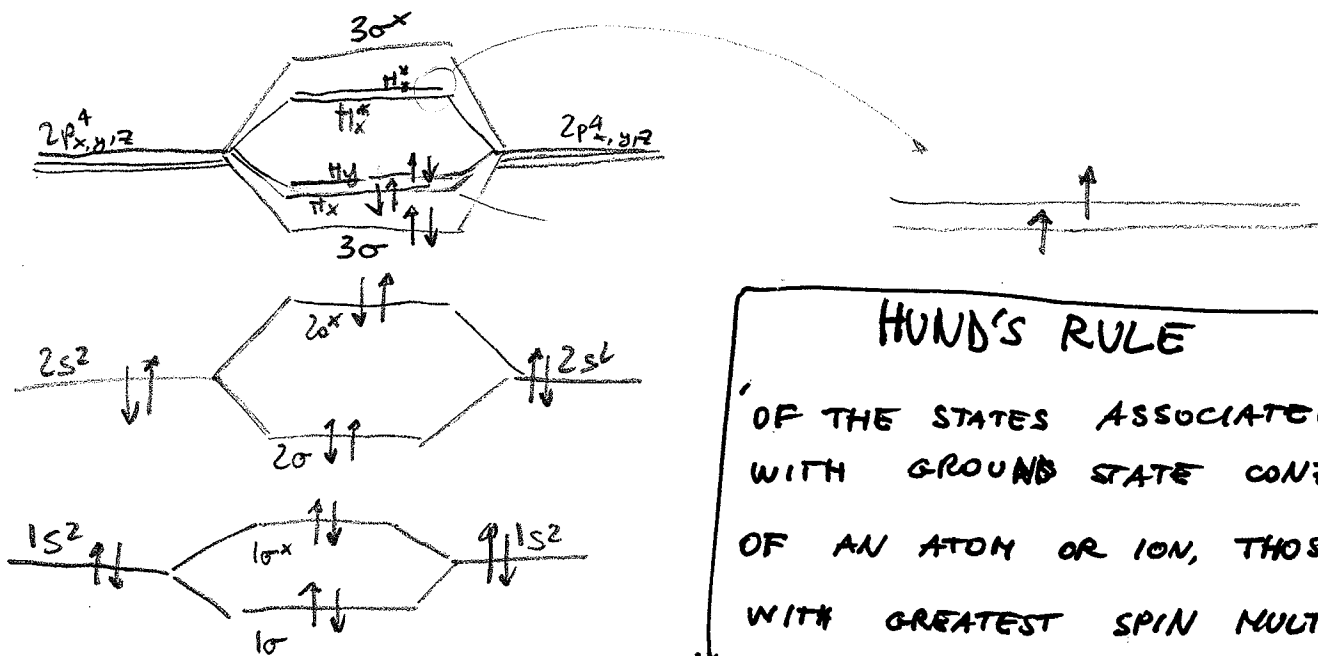


$E = \alpha - \beta$



OXYGEN O_2

$1s^2 2s^2 2p^4$
eighth electron:



HUND'S RULE
OF THE STATES ASSOCIATED WITH GROUND STATE CONFIGURATION OF AN ATOM OR ION, THOSE WITH GREATEST SPIN MULTIPLICITY LIE DEEPEST IN ENERGY

\Rightarrow LIFE $\Rightarrow O_2$ gets close to ENOGLOBING!
 $\Rightarrow O_2$ is PARAMAGNETIC, S_2 again

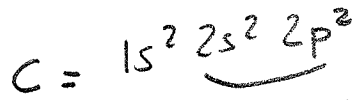
N_2 $1s^2 2s^2 2p^3$ is DIAMAGNETIC !!

F_2 $1s^2 2p^2 2p^5$ is DIA

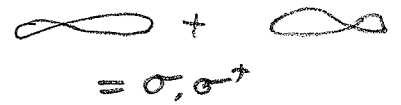
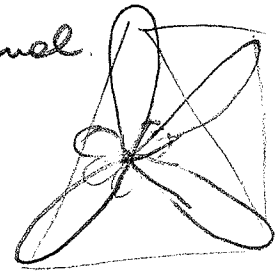
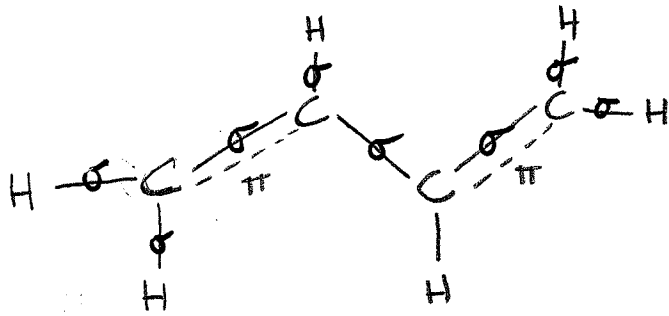
— FOR O_2, F_2 $3\sigma \downarrow$ of π

— FOR Li_2 to N_2 $\pi \downarrow$ then 3σ

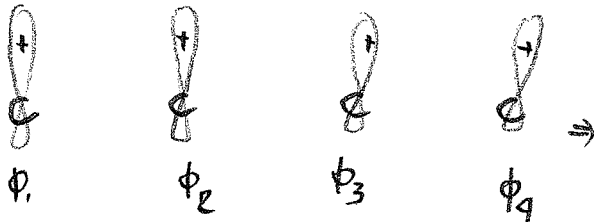
BUTADIENE



sp^3 tetrahedral



where are such π ? localized?



E

NODES

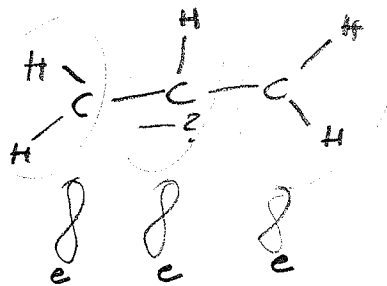
↑	3		$\psi = c_1\phi_1 - c_2\phi_2 + c_3\phi_3 - c_4\phi_4$	$\frac{3 + 1.6\beta}{}$
	2		$\psi = c_1\phi_1 - c_2\phi_2 - c_3\phi_3 + c_4\phi_4$	$\frac{2 - 0.6\beta}{}$
	1		$\psi = c_1\phi_1 + c_2\phi_2 - c_3\phi_3 - c_4\phi_4$	$\frac{\uparrow\downarrow}{2 + 0.6\beta}$
	0		$\psi_1 = c_1\phi_1 + c_2\phi_2 + c_3\phi_3 + c_4\phi_4$	$\frac{\uparrow\downarrow}{2 + 1.6\beta}$

delocalized

$$\begin{vmatrix} 2-E & \beta & 0 & 0 \\ \beta & 2-E & \beta & 0 \\ 0 & \beta & 2-E & \beta \\ 0 & 0 & \beta & 2-E \end{vmatrix} \Rightarrow X = \frac{2-E}{\beta} \begin{vmatrix} X & 1 & 0 & 0 \\ 1 & X & 1 & 0 \\ 0 & 1 & X & 1 \\ 0 & 0 & 1 & X \end{vmatrix}$$

ALLYL

PLANAR



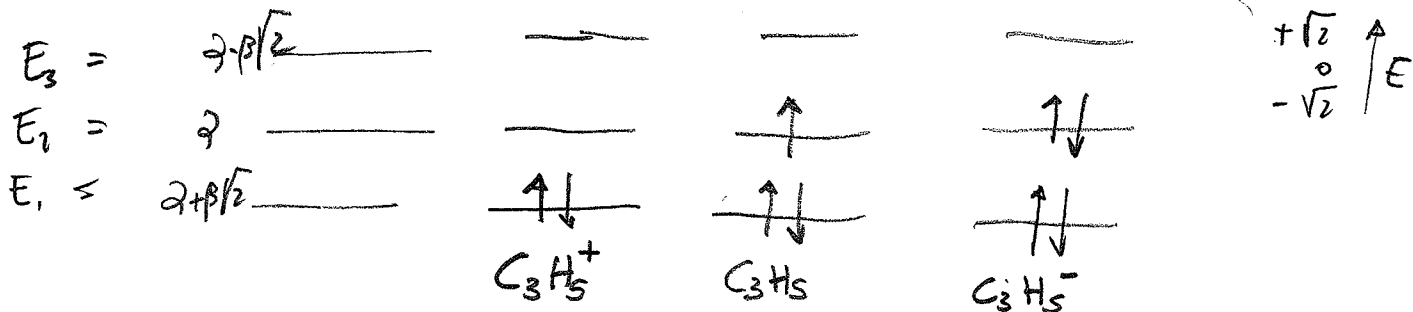
$$x = (2 - E) / \beta$$

$$\begin{vmatrix} x & 1 & 0 \\ 1 & x & 1 \\ 0 & 1 & x \end{vmatrix} \Rightarrow \det = 0$$

$$x^3 - 2x = 0 \quad \begin{cases} x = 0 \\ x = \sqrt{2}, -\sqrt{2} \end{cases}$$

$$x = \frac{2 - E}{\beta} \quad E = 2 - \beta x = \begin{cases} E = 2 \\ E = 2 \pm \sqrt{2}\beta \end{cases}$$

$\beta < 0$



c_1 ψ_1

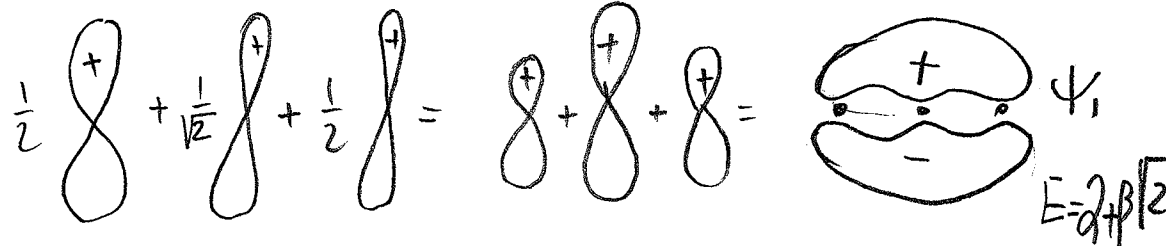
$$\begin{vmatrix} x & 1 & 0 \\ 1 & x & 1 \\ 0 & 1 & x \end{vmatrix} \begin{pmatrix} c_1 \\ c_2 \\ c_3 \end{pmatrix} = 0 \quad E_1 (x = -\sqrt{2}) \Rightarrow \begin{cases} c_1\sqrt{2} + c_2 = 0 \\ c_1 + c_2\sqrt{2} + c_3 = 0 \\ c_2 + c_3\sqrt{2} = 0 \end{cases}$$

remember $c_1^2 + c_2^2 + c_3^2 = 1$

$c_1 = c_3$ from (1)-(3)
 $c_2 = c_1\sqrt{2}$ from (2)

$$\frac{(1, \sqrt{2}, 1)}{\sqrt{1^2 + 2 + 1}} \Rightarrow \left(\frac{1}{2}, \frac{1}{\sqrt{2}}, \frac{1}{2}\right)$$

$$\psi_1 = \frac{1}{2}\phi_1 + \frac{1}{\sqrt{2}}\phi_2 + \frac{1}{2}\phi_3$$



ψ_2 ?

$$\left| \begin{array}{ccc|c} x & 1 & 0 & c_1 \\ 1 & x & 1 & c_2 \\ 0 & 1 & x & c_3 \end{array} \right| = 0 \quad \xrightarrow{x=0} \left. \begin{array}{l} c_2 = 0 \\ c_1 + c_3 = 0 \\ c_2 = 0 \end{array} \right\} \Rightarrow (1, 0, -1) \Rightarrow \left(\frac{1}{\sqrt{2}}, 0, -\frac{1}{\sqrt{2}}\right)$$

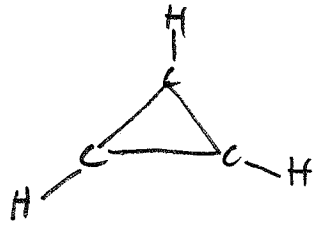
$$\Rightarrow \psi_2 = \frac{1}{\sqrt{2}}\phi_1 + 0\phi_2 - \frac{1}{\sqrt{2}}\phi_3 \Rightarrow$$

$$\frac{1}{\sqrt{2}}\begin{array}{c} + \\ \text{8} \end{array} + 0\begin{array}{c} + \\ \text{8} \end{array} - \frac{1}{\sqrt{2}}\begin{array}{c} + \\ \text{8} \end{array} = \begin{array}{c} + \\ \text{8} \end{array} + \begin{array}{c} - \\ \text{8} \end{array} = \begin{array}{cc} \begin{array}{c} + \\ \text{8} \end{array} & \begin{array}{c} - \\ \text{8} \end{array} \\ \begin{array}{c} - \\ \text{8} \end{array} & \begin{array}{c} + \\ \text{8} \end{array} \end{array} \quad E=2$$

$$\psi_3 \quad \left| \begin{array}{ccc|c} x & 1 & 0 & c_1 \\ 1 & x & 1 & c_2 \\ 0 & 1 & x & c_3 \end{array} \right| = 0 \quad \xrightarrow{x=\sqrt{2}} \left. \begin{array}{l} c_1\sqrt{2} + c_2 = 0 \\ c_1 + \sqrt{2}c_2 + c_3 = 0 \\ c_2 + \sqrt{2}c_3 = 0 \end{array} \right\} \Rightarrow \left(\frac{1}{2}, -\frac{1}{\sqrt{2}}, \frac{1}{2}\right)$$

$$\psi_3 = \frac{1}{2}\begin{array}{c} + \\ \text{8} \end{array} - \frac{1}{\sqrt{2}}\begin{array}{c} + \\ \text{8} \end{array} + \frac{1}{2}\begin{array}{c} + \\ \text{8} \end{array} = \begin{array}{c} + \\ \text{8} \end{array} + \begin{array}{c} + \\ \text{8} \end{array} + \begin{array}{c} + \\ \text{8} \end{array} = \begin{array}{ccc} \begin{array}{c} + \\ \text{8} \end{array} & \begin{array}{c} - \\ \text{8} \end{array} & \begin{array}{c} + \\ \text{8} \end{array} \\ \begin{array}{c} - \\ \text{8} \end{array} & \begin{array}{c} + \\ \text{8} \end{array} & \begin{array}{c} - \\ \text{8} \end{array} \end{array} \quad E=2-\beta\sqrt{2}$$

CYCLO PROPENIL



$$\begin{vmatrix} x & 1 & 1 \\ 1 & x & 1 \\ 1 & 1 & x \end{vmatrix} \Rightarrow 0 \quad \text{det}$$

$$x^3 - 3x + 2 = 0$$

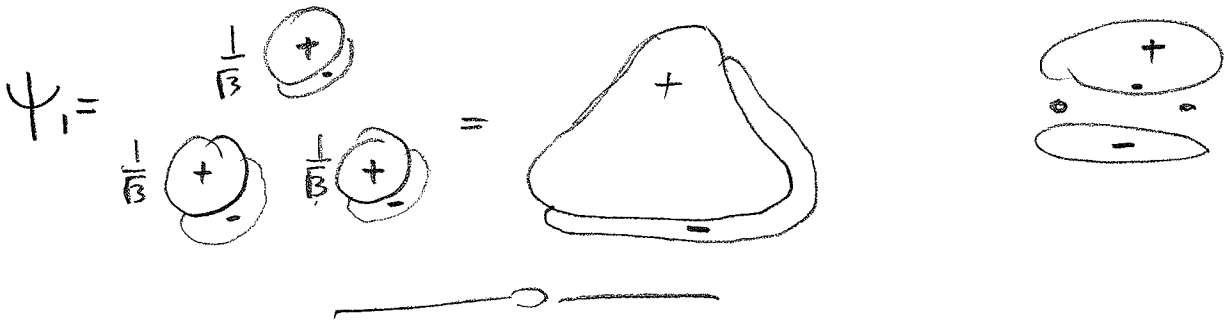
$$x = -2, +1, +1$$

+1 is double

$$E = \alpha - \beta x$$

$$E_1 = \alpha + 2\beta$$

$$x = -2 \quad \begin{vmatrix} -2 & 1 & 1 \\ 1 & -2 & 1 \\ 1 & 1 & -2 \end{vmatrix} \begin{pmatrix} c_1 \\ c_2 \\ c_3 \end{pmatrix} = 0 \quad \left(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}} \right)$$



$$E_2 = E_3 = \alpha + \beta$$

$$\begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} c_1 \\ c_2 \\ c_3 \end{pmatrix} = 0 \quad \downarrow \text{double}$$

$$c_1 + c_2 + c_3 = 0 \quad \leftarrow \text{plane } \perp (c_1 c_2 c_3)$$

$$c_1^2 + c_2^2 + c_3^2 = 1 \quad (\text{norm})$$

get 2

get 2 vectors in the plane $v_1 = (1, -1, 0)$

$$v_2 = (1, 0, -1)$$

and orthogonal

\Rightarrow

M11.

$|v_1| = 1$

$|v_2| = 1$

$v_1 = \left(\frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}, 0\right)$

$v_2 = \left(\frac{1}{\sqrt{2}}, 0, -\frac{1}{\sqrt{2}}\right)$

$v_1 \cdot v_2 = \frac{1}{2} \Rightarrow \text{not orthogonal} \Rightarrow$

$v_2^* \equiv v_2 - \frac{(v_1 \cdot v_2)}{\frac{1}{2}} v_1$

GRAM-SCHMIDT

$v_2^* \cdot v_1 = v_2 \cdot v_1 - \underbrace{(v_1 \cdot v_2)}_{\frac{1}{2}} \underbrace{(v_1 \cdot v_1)}_{1} = 0$

$v_2^* = \left(\frac{1}{\sqrt{2}}, 0, -\frac{1}{\sqrt{2}}\right) + \left(-\frac{1}{2\sqrt{2}}, +\frac{1}{2\sqrt{2}}, 0\right)$

$= \frac{1}{2\sqrt{2}}(1, 1, -2)$

$|v_2^*| = \sqrt{\frac{6}{4}} = \sqrt{\frac{3}{2}} = \frac{\sqrt{3}}{2}$

 \Rightarrow

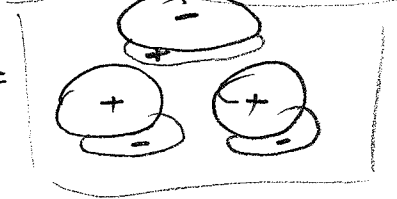
$v_2 = \frac{1}{\sqrt{6}}(1, 1, -2)$

$v_1 = \left(\frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}, 0\right)$

$\psi_2 =$



$\psi_3 =$



linear and all combinations!

 $\Rightarrow E$

$\frac{2-\beta}{\uparrow} \frac{2-\beta}{\downarrow} \alpha ?$

$\frac{2+2\beta}{\uparrow \downarrow}$

CYCLIC DEBYE HUCKEL

Linear chain N (open)

$$\begin{vmatrix} x_1 & & 0 \\ & \ddots & \\ 0 & & x_N \end{vmatrix} \Rightarrow$$

$$x_i = -2 \cos \left[\frac{i\pi}{N+1} \right] \Rightarrow c_{ij} = \sqrt{\frac{2}{N+1}} \sin \left(\frac{H_{ij}}{N+1} \right)$$

ORBITAL INDEX $i = [1, \dots, N]$
 ATOM INDEX $j = [1, \dots, N]$

$$E_i = \alpha - x_i \beta$$



Cyclic polyene



$$\begin{vmatrix} x_1 & & 0 \\ & \ddots & \\ 0 & & x_N \\ & & & x_1 \end{vmatrix} \Rightarrow$$

$$x_i = -2 \cos \left(\frac{2\pi i}{N} \right) \quad c_{ij} = \sqrt{\frac{1}{N}} e^{i \frac{2\pi i (j-1)}{N}}$$

• Real = unique

• complex

\Rightarrow degenerate, one has to be linear combination to have real coefficients

$$c_{ij} = \sqrt{\frac{1}{N}} e^{i \frac{2\pi i (j-1)}{N}}$$

$i = \text{ORBITAL } [1 \dots N]$
 $j = \text{ATOM } [1 \dots N]$

GRAPHICAL

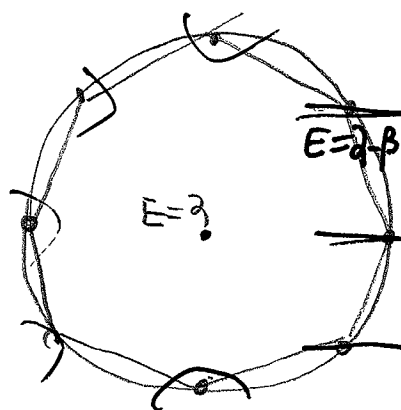
For linear : NO OFF DIAGONAL & "FIRST OFF DIAGONAL" elements \Rightarrow NO degenerate levels

N system

draw circle, centered at $E = \alpha$, radius $2|\beta|$

inscribe polyhedron with $(2m+2)$ carbons from the bottom

Allyl $n=3 \Rightarrow 2m+2=8$

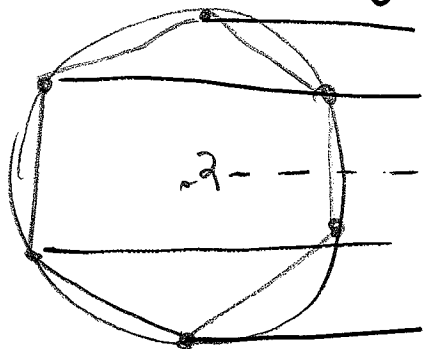


$E = \alpha - \beta/\sqrt{2}$ forget, bottom and up, and degeneracies

$E = \alpha$

$E = \alpha + \beta/\sqrt{2} \Rightarrow$ energies

For cyclic : inscribe polyhedron with N carbons
get degeneracies



$E_6 = \alpha + 2\beta$

$E_4, E_5 = \alpha - \beta$

$E_2, E_3 = \alpha + \beta$

$E_1 = \alpha + 2\beta$

no at $E = \alpha$
need
odd
number
of N .

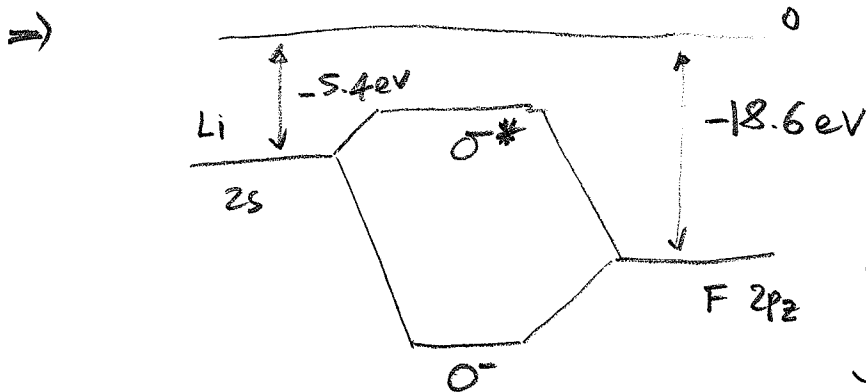
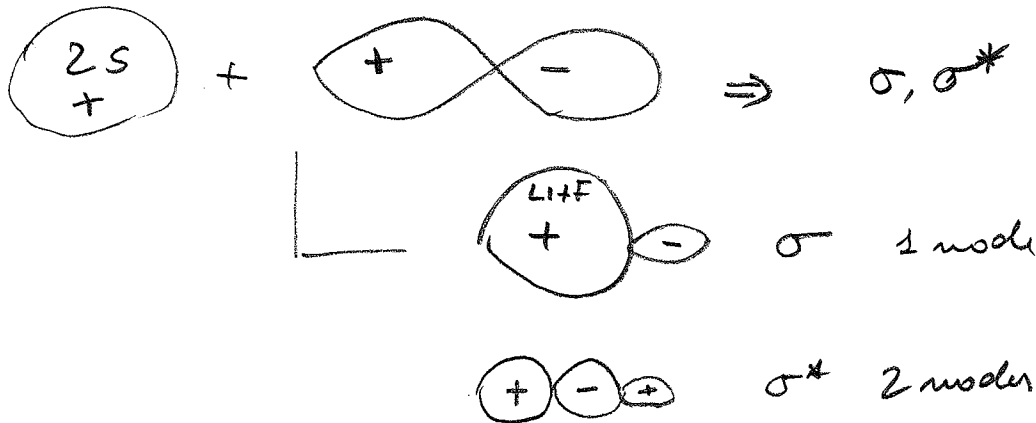
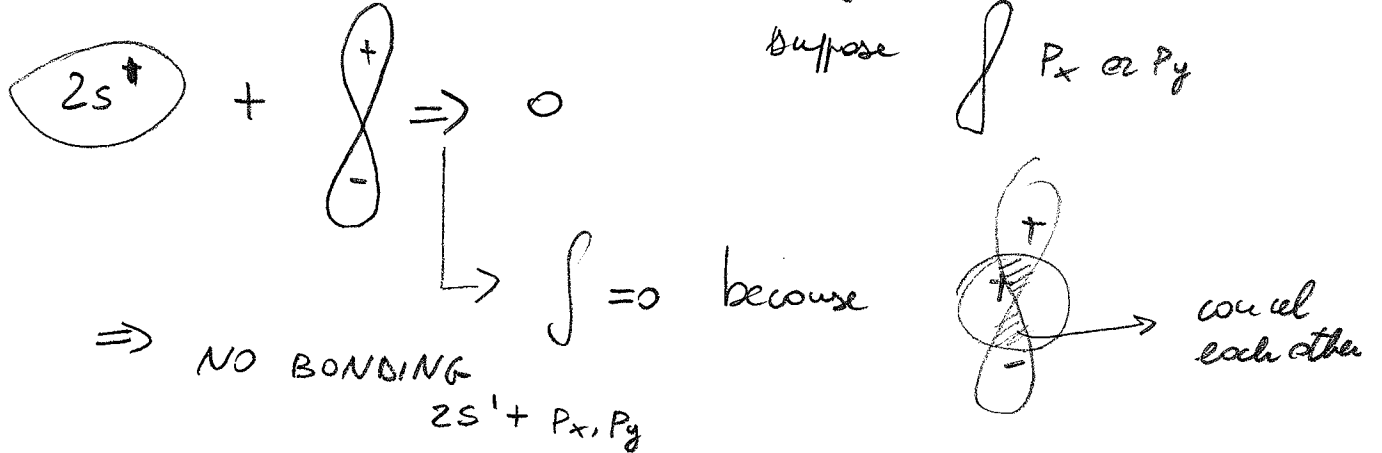
and fill 'em

BONDING OF ATOMS WITH DIFFERENT OVERLAP

LiF Lithium Fluorine

Li $1s^2 2s$

F = $1s^2 2s^2 2p^5 \Rightarrow$ only 1 e available

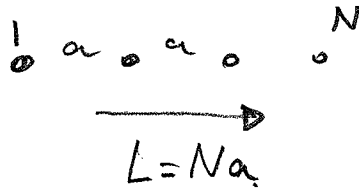


$$\psi = c_L \phi_L + c_F \phi_F$$

$$\psi_{\sigma^*} \Rightarrow c_L \gg c_F$$

$$\psi_{\sigma} \Rightarrow c_L \ll c_F$$

GENERALIZATION OF D.H for large N.



$N \gg 1 \Rightarrow \sim$ periodic
 expect results
 like periodic!

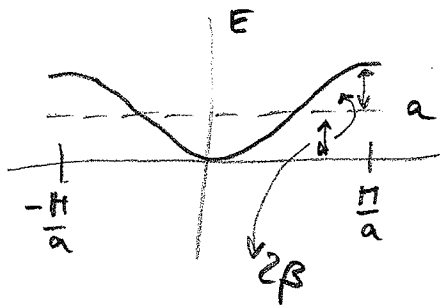
GS $\Rightarrow \psi = \sum_j c_j \phi_j \quad c_j = \sqrt{\frac{2}{N+1}} \sin\left(\frac{\pi j}{N+1}\right)$

$E = 2 + 2\beta \cos\left(\frac{\pi j}{N+1}\right)$

$N+1 \sim N \quad \frac{N}{j} \rightarrow \frac{Na}{ja} = \frac{L}{ja} \Rightarrow$

$c_j \sim \sqrt{\frac{2}{N}} \sin\left(\frac{\pi ja}{L}\right) \approx \sqrt{\frac{2}{N}} \sin(ka)$
 $k = \frac{\pi j}{L} \Rightarrow$
 $j=1, N \Rightarrow ka=0, \pi$

Remember $G^* =$ first Brillouin zone $= \frac{2\pi}{a} \Rightarrow BZ = \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$

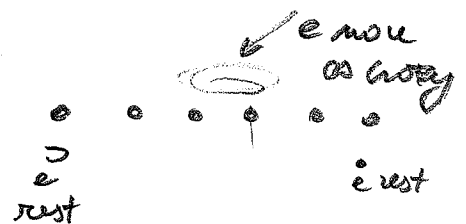
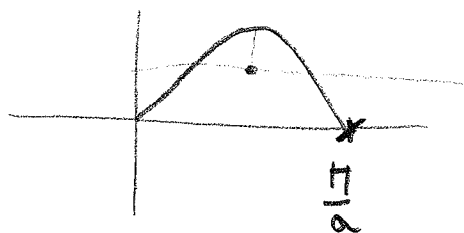


$E = 2 + 2\beta \cos(ka)$

$k = \left[0, \frac{\pi}{a}\right]$

$\sin(\frac{\pi}{2}) = 1$
 $\cos(\frac{\pi}{2}) = 0, -1$

$V_{group} = \frac{1}{\hbar} \frac{\partial E}{\partial k} = -\frac{2a\beta}{\hbar} \sin(ka)$



SOLUTION OF SCF

$$E_n = -\frac{13.6 Z^2}{n^2} \text{ valid only for Hydrogenoid}$$

with more electrons compute numerically

and get $E(n, e)$

: 1s 2s 2p 3s 3p 4s 3d 4p 5s 4d 5p 6s 5d 4f...

+ Fill up with HUND (level are splitted in m since L-S coupling \Rightarrow Zeeman)

but some orbitals have very close energy

2s & 2p \Rightarrow HYBRIDIZATION

HYBRIDIZATION of 2s & 2p

need of least ~~2p~~^{2s, 2p} but not too much: 1, 2, 3, 4, 6
 symmetries possible
 No 5

$$\text{Sum of } 2s\# + 2p\# < 5$$

Max $[\#(2s) + \#(2p)] = 6 \Rightarrow$ filled no HYB

or $[\#(2s) + \#(2p)] = 5 \Rightarrow$ no possible

$[\#(2s) + \#(2p)] = 4 \Rightarrow 4e \Rightarrow s^2 p^2 \Rightarrow sp^3 \Rightarrow sp^3 \text{ HYB}$
 Carbon

$[\#(2s) + \#(2p)] = 3 \Rightarrow 3e \Rightarrow s^2 p^1 \Rightarrow sp^2 \Rightarrow sp^2 \text{ HYB}$
 Boron

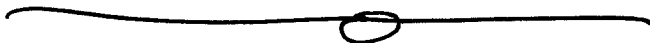
$[\#(2s) + \#(2p)] = 2 \Rightarrow 2e \Rightarrow s^2 p^0 \Rightarrow sp^1 = sp \text{ HYB}$
 Beryllium

H1 $[\#(2s) + \#(2p)] = 1 \Rightarrow$ NO HYB electrons
 only in 2s

HYBRIDIZATION

sp^1

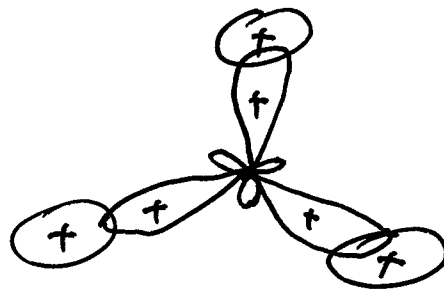
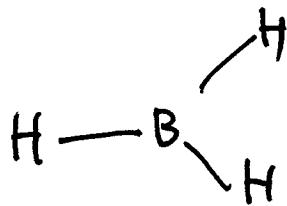
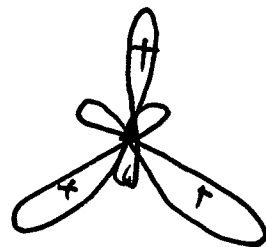
Be (or C in sp)



sp^2

B (or C in sp^2)
trigonal planar

sp^2



sp^3

C (diamond)

tetrahedron

